

String Theory

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- 1 From zero to one dimensional objects
- 2 String Theory
 - Classical and quantum version of String Theory
 - Classification of superstring models
 - Higher dimensional theories
 - Compactification
- 3 Building models
- 4 Conclusion

Plan

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Particle Physics

- Fundamental Interactions of Nature
 - Electromagnetic interaction :
 - Strong interaction :
 - Weak interaction :
 - Gravitation theory
- Gauge Theories
 - Grand Unified theory (GUT) :
 - Gauge Symmetries :

Particle Physics

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Particle Physics

- **Fundamental Interactions of Nature**
 - Strong interaction : $su(3)$ Lie algebra
 - Weak interaction : $su(2)$ Lie algebra
 - Electromagnetic interaction : $u(1)$ Lie algebra
 - Gravitation theory : **Geometric deformation of the univers**
- **Gauge Theories**
 - Grand Unified theory (GUT) : $E_6, so(10), su(5)$ Lie algebras
 - ① Electromagnetic interaction
 - ② Strong interaction
 - ③ Weak interaction
 - Gauge Symmetries : $A_n D_n E_{6,7,8}$ Lie algebras

Lie algebras in particle physics

- Lie structure
- Representation theory
- Coxter and Dynkin diagrams
- Cartan matrices

Secrets of Nature are hidden in Lie algebra structures

The main problem is the gravity theory

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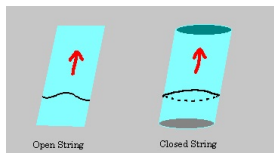
The motion of particles (zero dimensional objects) should be extended to the motion of one dimensional objects : **strings**

- **Two configurations**
 - 1 Open string theory
 - 2 Closed string theory

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Classical string theory

The action of the classical theory

$$S = \frac{1}{2\pi\alpha'} \int d\tau d\sigma \left(\frac{\partial X^\mu}{\partial \tau} \frac{\partial X_\mu}{\partial \tau} - \frac{\partial X^\mu}{\partial \sigma} \frac{\partial X_\mu}{\partial \sigma} \right)$$

Quantum theory

- The quantization gives

$$(g_{\mu\nu}, B_{\mu\nu}, A_\mu, \phi, \dots)$$

- Graviton, photons,.....

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First revolution

Superstring models

- Models beyond particle physics
- 5 models
 - ① Type IIA
 - ② Type IIB
 - ③ Heterotic superstring theory with $SO(32) = D_{16}$ gauge symmetry
 - ④ Heterotic superstring theory with $E_8 \times E_8$ gauge group
 - ⑤ Type I with $SO(32) = D_{16}$ gauge symmetry.
- Dimension of the space-time : $D = 10$
- Gauge symmetries (Lie algebras) :
 - ① $E_8 \times E_8$
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Second revolution

Problems and partial solutions

- Many problems !
 - 1 Space-time dimension : $D = 10 > 4$
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 - 3 Large gauge symmetries : $SO(32) = D_{16}, E_8 \times E_8$
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- Partial solutions
 - Compactification
 - $D = 10 \rightarrow D = 4$
 - String dualities
 - Connection between string models in lower dimensions
 - New theories
 - 1 M-theory in $D = 11$, Witten, 1995
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Compactification of higher dimensional theories

Compactification

- Four dimensional models

$$R^{1,D-1} \rightarrow R^{1,3} \times X^{D-4}$$

$X^{D-4} = (D - 4)$ -dimensional compact manifolds.

- 1 String theory lives in $D = 10$
 - $10 = 4 + 6$
- 2 M-theory lives in $D = 11$
 - $11 = 4 + 7$
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Toroidal Compactification of superstring theory

String theory

- Compactification

$$R^{1,9} \rightarrow R^{1,3} \times X^6$$

X^6 =6-dimensional compact manifolds.

- $X^6 = T^2 \times T^2 \times T^2$.

Toroidal Compactification of superstring theory

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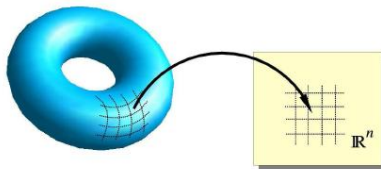
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Connection with particle physics

Calabi-Yau manifolds

- Calabi-Yau compactification

$$R^{1,9} \rightarrow R^{1,3} \times X^6$$

$X^6 =$ 3- dimensional Calabi-Yau manifolds.

- 1 Kahler manifolds
 - 2 $SU(3)$ holonomy group
 - 3 $\Omega = dz_1 dz_2 dz_3,$
- Constructions of Calabi-Yau manifolds
 - 1 Orbifolds : $T^6/G, G \subset SU(3)$
 - 2 Hypersurfaces in $CP^4(z_1, z_2, z_3, z_4, z_5)$ projective space

$$P_5(z_1, z_2, z_3, z_4, z_5) = 0$$

- 3 Hypersurfaces in toric varieties, using toric geometry method.

Connection with particle physics

Calabi-Yau manifolds

- Calabi-Yau compactification

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$X^6 =$ 3- dimensional Calabi-Yau manifolds.

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 - 2 Hypersurfaces in $CP^4(z_1, z_2, z_3, z_4, z_5)$ projective space

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- 3 Hypersurfaces in toric varieties, using toric geometry method.

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$X^7=7$ -dimensional compact manifolds.

- 1 T^7, \dots
- 2 G_2 manifolds (Standard model)

- G_2 manifolds

- 1 7-dimensional real manifolds
- 2 G_2 holonomy group
- 3 Special 3-form

$$w = f_{ijk} dx_i dx_j dx_k$$

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$$t_i t_j = -\delta_{ij} + f_{ijk} t_k$$

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 - Classical and quantum version of String Theory
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